

Program Information		[Les	son Title]		TEACHER NAME Julie Thumann		PROGRAM NAME Cincinnati City Schools	
	Li	[U near Functions	nit Title] s Interactive Note	book	NRS EFL(s) 3 – 6		TIME FRAME 4 – 7 classes (75 minutes each)	
			<u>OB</u> F	R ABE/ASE S	tandards – M	athematics		
	Numbers (N)		Algebra (A)		Geometry (G)		Data (D)	
Instruction	Numbers and Operation		Operations and Algebraic Thinking		Geometric Shapes and Figures		Measurement and Data	
	The Number System	N.4.1	Expressions and Equations	A.4.9 A.4.10 A.5.6 A.5.9	Congruence		Statistics and Probability	
	Ratios and Proportional Relationships	N.3.32	Functions	A.4.12 A.4.13 A.4.14 A.4.15 A.5.11 A.5.13 A.6.7	Similarity, Right Triangles. And Trigonometry		*Benchmarks identi priority benchmarks Curriculum Alignme the <u>Teacher Resou</u> complete list of prio and related Ohio Al	fied in red are s. Please see the ents available on <u>rce Center</u> for a rity benchmarks BLE lesson plans.
	Number and Quantity				Geometric Measurement and Dimensions			



	Mc Ge	odeling with cometry		
Mathen	natical	Practices (MP	)	
<ul> <li>Make sense of problems and persevere in solving them. (MP.1)</li> </ul>	~	Use appropria	ate tools strategical	lly. (MP.5)
✓ Reason abstractly and quantitatively. (MP.2)		Attend to prec	cision. (MP.6)	
<ul> <li>Construct viable arguments and critique the reasoning of others. (MP.3)</li> </ul>		Look for and r	make use of struct	ure. (MP.7)
✓ Model with mathematics. (MP.4)	✓	Look for and e	express regularity i	in repeated reasoning. (MP.8)
LEARNER OUTCOME(S)	AS	SESSMENT TO	OOLS/METHODS	
<ul> <li>Students will be able to:</li> <li>Determine the slope of a line from a graph, equation, or table</li> <li>Interpret unit rate as the slope in a proportional relationship of real-world and mathematical problems</li> <li>Complete a table of x-and y-values for a linear equation</li> <li>Use x-and y-values to graph a linear equation</li> <li>Graph linear equations to solve real-world problems</li> </ul>		<ul> <li>Student responses to teacher questions during class discussions</li> <li>Checks for understanding</li> <li>Teacher observation of student work</li> <li>Student answers to in-class assignments</li> <li>Assessment #1 (Vocabulary Review, Skill Review, Skill Practice) from <u>Common Core Achieve: Mastering Essential Test Readiness</u> Skills (Mathematics) pgs. 156 – 157</li> <li>Assessment #2 (Vocabulary Review, Skill Review, Skill Practice) from <u>Common Core Achieve: Mastering Essential Test Readiness</u> Skills (Mathematics) pgs. 164 – 165</li> <li>Assessment #3 (Vocabulary Review, Skill Review, Skill Practice) from <u>Common Core Achieve: Mastering Essential Test Readiness</u> Skills (Mathematics) pgs. 164 – 165</li> <li>Assessment #3 (Vocabulary Review, Skill Review, Skill Practice) from <u>Common Core Achieve: Mastering Essential Test Readiness</u> Skills (Mathematics) pgs. 170 - 171</li> </ul>		
LEARNER PRIOR KNOWLEDGE				
• Knowledge of fractions, integers, number lines, and coord	dinate	plane		
<ul> <li>Evaluate an expression (plug-in given numbers to solve for</li> </ul>	or the u	unknown variabl	le)	



This lesson begins with a review of prior knowledge; referencing integers and coordinate plane					
INSTRUCTIONAL AC	TIVITIES	RESOURCES			
1. Pass out Integ	<u>ers Foldable Layered-Look Book</u> handout.	Notebooks or folders for student use			
a. Mode the fo	folding instructions and provide supplies for students to create dable.	Student copies of Integers Foldable Lavered-Look Book			
b. Comp	lete the <u>Integers Foldable Layered-Look Book</u> as a class.	handout (attached)			
i.	Model how to solve example problems.				
ii.	Collaborate for writing the rule summary on the bottom of each page.	Stapler for student use			
iii.	Glue or staple the completed <i>Integers Foldable Layered-Look</i> <u>Book</u> into your notebook.	Glue sticks for student use			
2. Interpret Slope	e and Linear Functions	Projector/ability to project			
a. Introd	uction:				
i.	Slope, a measure of the steepness of a line, is the ratio of vertical change to horizontal change (or rise over run).	Chalkboard or whiteboard			
ii.	We are able to measure slope on a coordinate plane.	Our dans and in a formation of Ordered Dairs (attached o			
iii.	Let's discuss a real-life example of a coordinate plane – city streets. In many cities, streets that run east and west are	handouts per page)			
	named with numbers, and streets that run north and south are named with letters. Due to this convenient naming system, it is easy for people to navigate in an unfamiliar city and find their locations.	Student copies of <i>Interpreting Slope From a Graph or Table</i> booklet (attached)			
iv.	Let's take a look at a coordinate plane.	Assessment-on-a-stick for student use (attached)			
b. Pass out Graphing Ordered Pairs handout.					
i.	Label as a class. Discuss how grid is similar to the city street example – the east and west is the horizontal x-axis, and the	Student copies of <i>Linear Relationships</i> graphic organizer (attached)			
	have seen this grid in other real-life situations?	West Virginia Board of Education: Frayer Model. (n.d.).			
ii.	Glue or staple Graphing Ordered Pairs handout into your	https://wvde.state.wv.us/strategybank/FrayerModel.html			



notebook.		
<ul> <li>Now, add the lesson's vocabulary words and definitions in your notebook:</li> </ul>	Student copies of Math Talk Bookmark (attached)	
<ul> <li>Coordinate plane – a grid formed by the intersection of a horizontal number line and a vertical number line</li> </ul>	Student copies of Math Talk Bookmark (attached) Math Talk Bookmark. (n.d.). Retrieved from	
<ul> <li>ii. Quadrant – 1 of the 4 regions of the coordinate plane formed by the intersection of the x and y axis</li> </ul>	Otudent en in et lineen en Merlineen Cerd	
<ul> <li>iii. Ordered pairs – a pair of numbers (x,y) that is used to describe the location of a point on a coordinate grid</li> </ul>	(attached)	
<ul> <li>iv. Slope – the ratio of vertical change to horizontal change</li> <li>v. Unit rate – a rate that compares to one unit, such as mile per gallon</li> </ul>	Student copies of <i>All Linear Patterns</i> handout (attached, 2 per page)	
d. Next, we will begin a new page in the notebook titled Interpreting Slope From a Graph or Table	Using the Think-Pair-Share Technique-ReadWriteThink.	
3. Interpreting Slope From a Graph or Table handout	http://www.readwritethink.org/professional-	
<ul> <li>Pass out Interpreting Slope From a Graph or Table handout. Model folding instructions and provide supplies for students to create the foldable.</li> </ul>	development/strategy-guides/using-think-pair-share- 30626.html	
<i>i.</i> This handout will need to be <u>folded vertically and then</u> <u>accordion-style</u> .	Student copies of <i>Slope and Intercept Practice</i> foldable (attached)	
ii. Glue or staple <i>Interpreting Slope From a Graph or Table</i> handout into your notebook	Student copies of X-Intercent (attached)	
b. Add the definition for slope to your notebook:		
<ul> <li>Slope should always be reported in the proper units: <u>Dependent variable units (y-axis)</u></li> </ul>	Student copies of Y-intercept (attached)	
Independent variable units (x-axis) ii. The slope of the line represents the ratio of change in the dependent variable/y-axis/rise to the change in the independent variable/x-axis/run.	Student copies of the <i>Linear Equations Flippables</i> (attached)	
c. Whole class discussion and completion of <i>Slope From a Graph or Table</i> handout.	Common core achieve: Mastering essential test readiness skills (Mathematics). (2015). Columbus, OH: McGraw-Hill Education	
i. Write on the board, "We will now be able to answer the		



<ul> <li>question how do you calculate the rate of change on a linear model?" The model today is a table or graph. Refer to the completed <i>Slope From a Graph or Table</i> handout for class examples.</li> <li>i. Model the first example, <i>Paul's Job</i>. Check student understanding using the Happy/Sad Face Assessment-on-a-Stick or Thumbs Up/Thumbs Down.</li> </ul>	Zike, D. (n.d.). <i>Teaching Mathematics with Foldables</i> . Retrieved from <u>https://blogs.edutech.nodak.edu/badlandsreadingcouncil</u> <u>/files/2012/03/math-foldables.pdf</u>
Oil Tank, Todd's Account, Delivery Service Charges, Donna's Yard Service) and review answers as a class.	
4. Analyze Linear and Nonlinear Relationships	
a. Pass out the Linear Relationships graphic organizer to define linear.	
<ol> <li>Explanation of a linear relationship will be defined and completed together – write the template on the board or project the template on a whiteboard.</li> </ol>	
<ul> <li>As you complete the graphic organizer with the class, ask students to also explain nonlinear (use phrases from the <i>Math</i> <i>Talk Bookmark</i> to solicit student responses and check student understanding).</li> </ul>	
b. Linear or Nonlinear Card Sort	
i. Pass out Linear or Nonlinear Card Sort envelopes.	
<ol> <li>Instruct students to make a t-chart in their notebooks. Label one side of the t-chart "Linear" and the other side of the t-chart "Nonlinear"</li> </ol>	
<ol> <li>Each envelop should contain 4 graphs and 4 tables. Students are to identify each graph and table as linear or nonlinear and glue or tape the graph or table into the correct column in their notebook.</li> </ol>	
3. Walk around the room to observe student work and answer student questions (use phrases from the <i>Math Talk Bookmark</i> to solicit student responses and check student understanding).	
ii. Review correct answers.	



	1.	How do linear and nonlinear functions change the data?	he
	2.	Which function has a constant change in rate?	
	3.	Why would data be important in real-life situatio	ons?
	4.	Which interpretation is easier to comprehend, th graph or table?	ne
5. All Lin	ear Patterns han	dout	
a.	Pass out All Lin four patterns to	near Patterns handout. Each student should recein solve and continue the pattern.	ive
b.	Model how to s	olve one of the patterns.	
C.	For the remain complete. Rem purpose of this	ng patterns, have students use Think-Ink-Pair-Shind students that $f(x)$ means function. However, lesson $f(x)$ is like the y.r	hare to for the
	i. Studer	ts think about the problem.	
	ii. Studer	ts write down their answers.	
	iii. Studer	ts pair with a partner to discuss.	
	iv. Studer the cla probler	ts share with their partner and share out to the re ss the correct answer and how they solved the n.	est of
6. Slope	and Intercept Pra	actice	
a.	To help graph a understand the students to sta Intercept Pract	and comprehend the equations students need to importance of the x and y intercepts. Instruct you t a new page in their notebooks and title it <i>Slope</i> ice.	ur e and
	i. Teache Interce	er will need to print out the following: <i>Slope and pt Practice</i> foldable, <i>X-Intercept</i> , <i>Y-intercept</i> .	
	ii. Before fold.	class, cut-out the x and y intercept rectangles, ar	nd
a.	Each student n out.	eeds one x-intercept cut out and one y intercept of	cut
b.	Ask students to <i>Practice</i> .	glue these under the title, Slope and Intercept	



c. Re	efer to completed, Slope and Intercept Practice foldable.	
d. W sti int	Trite these ordered pairs on the board: (-2,-2) and (1,4). Have udents plot the points and then record the x-intercept and the y-tercept and the slope.	
e. Fo 1)	pllow the same procedure for the next ordered pairs: (-4,0) and (0,-	
f. Di fir ar to	iscuss the difference between a positive and negative slope. The st example is a positive slope - the line rises from the left to the right the second example has a negative slope – lines that fall from left right.	
7. Write the	Equation of a Line	
a. Th us th	ne equation of a line can be written many different ways. You can se given information about the line to determine the best way to write e equation.	
b. A cc ea us to th yc	good example of this is a cell phone bill. Some cell phone ompanies charge an initial fee and then add additional changes for ach byte of data used. To find the total cost of your monthly bill you se the same formula used to write the equation of a line. If you were graph this information, your graph would be a line that describes e relationship between the data used and the total monthly cost of bur cell phone.	
c. To	oday we will use two different formulas to write an equation.	
	i. Pass out the Linear Equations Flippables.	
	<ul> <li>Model folding instructions and provide supplies for students to create the foldable.</li> </ul>	
	iii. Present and explain examples for each formula. Then provide more examples on the board and remind students to write the examples in their notebooks. Students will use the <i>Linear</i> <i>Equations Flippables</i> for reference.	
	iv. Examples for Slope-Intercept Form: y=mx+b	
	<ol> <li>Write the equation of the line with the slope of -5 and y-intercept of 4.</li> </ol>	
	a. Step 1: identify m= -5, b=4	



<ul> <li>b. Step 2: use these values to write the equations: y=5x+4</li> <li>2. A line has a slope of 3 and contains the points (2,7)</li> <li>a. Step 1: m=3, x=2, y=7</li> </ul>
2. A line has a slope of 3 and contains the points (2,7)
2. Stop 1: $m = 3 \times 2 \times 2 \times 7$
a. Step 1. $m=3, x=2, y=7$
b. Step 2: solve to find the value of b.
7=3(2) + b
7=6 + b
1=b
c. Therefore: y=3x + 1
v. Example for the Point – Slope Form: y-y=m(x-x)
1. A line has a slope of 1 and contains the point (4, -3)
a. Step 1: Substitute the values: y-(-3)=1(x-4)
b. Step 2: y+3=x-4
c. Step 3: Subtract 3 from both sides: y=x-7
vi. Example for Slope Formula: write an equation given two points
1. A line contains the points (4,-4) and (3,0)
a. Step 1: Find the slope using the Slope Formula: m=-4-0=-4=-4
4-3=1
<ul> <li>b. Step 2: Now that you know the slope you may use either formula to write the equation, and choose only one of the given points.</li> </ul>
Y=mx+b
0=-4(3)+b
0=-12+b
12=b
c. Step 3: Plug in for m and b
Y=-4x+12
8. Have students complete Assessment #1 (Vocabulary Review, Skill Review,



		Olill Deseties) from Common Core Achieve: Machanian Ecoeptial Test	
		Skill Practice) from Common Core Achieve: Mastering Essential Test	
		<u>Readiness Skills (Mathematics)</u> pgs. 156 – 157, Assessment #2 (vocabulary	
		Review, Skill Review, Skill Practice) from <u>Common Core Achieve: Mastering</u>	
		Essential Test Readiness Skills (Mathematics) pgs. 164 – 165, Assessment	
		#3 (Vocabulary Review, Skill Review, Skill Practice) from <u>Common Core</u>	
		Achieve: Mastering Essential Test Readiness Skills (Mathematics) pgs. 170 –	
		171 in class or for homework. Students may use their Interactive Notebook for	
		the assessments.	
	9.	Once complete review and discuss the answers in class or collect the	
		assessments to check and review with students individually.	
	DIFFE	RENTIATION	
	•	Provide students with partially complete handout, graphic organizer, and/or foldab	les
	•	Display written vocabulary terms and definitions	
	•	Allow students to work individually, in pairs, or in class groups	
	TEAC	HER REFLECTION/LESSON EVALUATION	
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Ř	ADDIT	TIONAL INFORMATION	



## Adding Integers with the SAME SIGN

Example 1:	Model:
5 + 7 =	
Example 2:	Model:
-5 + (-7) =	

#### Multiplying & Dividing Integers with DIFFERENT SIGNS



Summary:

× Multiplying & Dividing ÷

### <u>Rule</u>: To subtract an integer,

\_\_\_\_\_

Example 5:  

$$12 - (-7) =$$
  
Example 6:  
 $-9 - 4 =$   
Example 7:  
 $-15 - (-3) =$   
Example 8:  
 $7 - 10 =$ 

Summary:

Г

#### Multiplying & Dividing Integers with the SAME SIGNS



## Adding Integers with DIFFERENT SIGNS

Example 3:	Model:
-5 + 7 =	
Example 4:	Model:
5 + (-7) =	

Summary:

## + Adding +







#### Multiplying & Dividing Integers with DIFFERENT SIGNS

Multiplying	Dividing				
Example 13: $-4(9) = -36$	Example 15: $-49 \div 7 = -7$				
Example 14: 8(-7) = -56	Example 16: $\frac{64}{-4} = -16$				
Summary: When multiplying or dividing: If the + + = + signs are the same, the answer is = + positive. If the signs are + - = - different, the answer is negative + = -					
× Multiplying $\alpha$ Dividing $\div$					

#### <u>Rule</u>: To subtract an integer,

"Keep, Change, Change" or "Add the Opposite"

Example 5:  

$$12 + (+7) = 19$$
  
Example 6:  
 $-9 + 4 = -13$   
Example 7:  
 $-15 + (+3) = -12$   
Example 8:  
 $7 + 10 = -3$ 

Summary: When subtracting, change the subtraction sign to addition and switch the sign of the next integer. Now it's an addition problem and you will use the same rules as we did for addition.

## -Subtracting -

#### Multiplying & Dividing Integers with the SAME SIGNS



### Adding Integers with DIFFERENT SIGNS

Example 3:		Model: Zero Pairs!
-5 + 7 =	2	= Positive 2
Example 4:		
5 + (-7) =	-2	Negative 2
Summary:	If the If the the sig	signs are the same, add and keep their sign. signs are different, find the <i>difference</i> , then take n of the integer with the larger absolute value.

+ Adding +

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#### Directions for putting together the integer foldable!

<u>Stepı</u>:

Print pages 1 & 2 front to back as shown:



Print pages 3 & 4 front to back as shown:



<u>Step 2</u>: Place the page that says "Multiplying & Dividing" (at the very bottom) face up on your desk.

<u>Step 3</u>: Place the page that says "Subtracting" (at the very bottom) face up on top of the other page, so that you can just see the bottom of the original page, as shown:



<u>Step 4</u>: Fold over both pages so that "Adding" is just above where is says "Subtracting" and the "Integers" title is at the very top.

Step 4: Staple and you're done!







## GRAPHING ORDERED PAIRS





Length of Spring (in inches)	Weight (in pounds)
4.0	0.0
4.8	0.5
5.6	1.0
6.4	1.5
7.2	2.0





Delivery Service Charges		
Miles Traveled Charge		
00.41\$	τ	
00.12\$	2	
\$28.00	ε	
¢32'00	4	

# INTERPRETING SLOPE FROM A GRAPH OR TABLE



<b>(1)</b>	
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Hours Worked	Amount Charged
1	\$11
2	\$17
3	\$23
4	\$29
5	\$35





## Linear Relationships



Linear Relationships graphic organizer

• I agree/disagree with you because ...

· Math Talk 🛧 ·

- What I heard you say was...
- What key words helped you solve this?
- Can you explain this to me?
- What were you thinking here?
- How did you solve it?
- What did you start with?
- Why did you choose that operation?

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- What strategy did you use?
- Why did you choose that strategy?
- How did you know your answer was right?
- Prove your answer is right.
- How else can you solve it?

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- How did this help you understand?
- How is this like other problems you've solved?

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• Math Talk ★ • • I agree/disagree with you because ... . What I heard you say was... . What key words helped you solve this? • Can you explain this to me? • What were you thinking here? . How did you solve it? • What did you start with? • Why did you choose that operation? • What strategy did you use? • Why did you choose that strategy? . How did you know your answer was right? · Prove your answer is right. . How else can you solve it? How did this help you understand? • How is this like other problems you've solved? 0 0 





#### The function f(x) is linear.

x	f(x)
-3	8
-1	11
1	14

A functional relationship is shown in this table.

x	0	1	2	3
f(x)	-1	1	3	?

What is the value of the function when x is 3?

What is the value of <i>f</i> (5)?	
<b>F</b> —5	
•	

3 G

**H** 17

J 20

The function f(x) is linear.

**A** 3

**B** 4

**C** 5

**D** 6

x	-10	-5	0	5
f(x)	-4	-1	2	5

What is the value of f(15)

F	15	н	11
G	12	J	8

The function f(x) is linear.

x	f(x)
-2	-9
-1	-5
0	-1

#### What is the value of f(2)?

Α -6 2 в 3 С D 7

#### The function f(x) is linear.

x	f(x)
-3	8
-1	11
1	14

A functional relationship is shown in this table.

x	0	1	2	3
f(x)	-1	1	3	?

What is the value of the function when x is 3?

W	hat i	s the value of <i>f</i> (5)?
F	-5	
G	3	
Н	17	
J	20	The function

The	function	f(x)	is	linear

**A** 3

**B** 4

**C** 5

**D** 6

x	-10	-5	0	5
f(x)	-4	-1	2	5

What is the value of f(15)

F	15	н	11
G	12	J	8

The function f(x) is linear.

x	f(x)
-2	-9
-1	-5
0	-1

What is the value of f(2)?

- A −6
- 2 в
- 3 С
- D 7

1	14	
lue c	of f(5)?	

Y-Intercept: X-Intercept: Slope:

	1	
x	0	
	۸.	

Slope: X-Intercept: Y-Intercept:



Slope: X-Intercept: Y-Intercept:

x	0	
	• • •	

Slope: Y-Intercept: Y-Intercept:

	<b>A</b>	
X	0	
	1 A	



Slope: X-Intercept: Y-Intercept:



Slope:	
X-Intercept:	
Y-Intercept:	

Slope and Intercept Practice

X-Intercept		X-Intercept
The point where a graph crosses the	•	
X-Intercepts happen when the	is	X-Intercepts happen when the is is
To find the x-intercept from an (or) with and solve for	, replace 	To find the x-intercept from an, replace, (or) with and solve for
X-Intercent		X-Intercept
The point where a graph crosses the		The point where a graph crosses the
X-Intercepts happen when the	is	X-Intercepts happen when the is
To find the x-intercept from an (or) with and solve for	, replace	To find the x-intercept from an, replace, (or) with and solve for
 X Intercent		X-Intercept
The point where a graph crosses the		The point where a graph crosses the
X-Intercepts happen when the	is	X-Intercepts happen when the is
To find the x-intercept from an (or) with and solve for	, replace	To find the x-intercept from an, replace (or) with and solve for
X		X-Intercept
The point where a graph crosses the		The point where a graph crosses the
X-Intercepts happen when the	is	X-Intercepts happen when the is
To find the x-intercept from an (or ) with and solve for	, replace	To find the x-intercept from an, replace (or) with and solve for

, — - ,	Y-Intercept	、	,	Y-Intercept	,
The p	oint where a graph crosses the	<sup>.</sup> I	The	point where a graph crosses the	· I
l Y-Inte	rcepts happen when the	is	l Y-Int	tercepts happen when the	is
To fin	d the y-intercept from an and solve for	_, replace I	To fi	nd the y-intercept from an and solve for	, replace I
,	Y-Intercept	、	,	Y-Intercept	,
The p	oint where a graph crosses the	<sup>.</sup> I	The	point where a graph crosses the	· I
l Y-Inte	rcepts happen when the	is I	l Y-Int	tercepts happen when the	is I
To fin	d the y-intercept from an and solve for	_, replace	To fi	ind the y-intercept from an	, replace
, !	Y-Intercept	,	,	Y-Intercept	、
The p	oint where a graph crosses the	· [	The	point where a graph crosses the	· I
I Y-Inte	rcepts happen when the	is I	l I Y-Int	tercepts happen when the	is I
To fin	d the y-intercept from an and solve for	_, replace /	To fi	nd the y-intercept from an	, replace I
, i	Y-Intercept	、	,	Y-Intercept	、
The p	oint where a graph crosses the	· [	The	point where a graph crosses the	·
l Y-Inte	rcepts happen when the	_ is I	l Y-Int	tercepts happen when the	is I
To fin	d the y-intercept from an	_, replace	To fi	ind the y-intercept from an	, replace











![](_page_35_Figure_0.jpeg)

![](_page_36_Figure_0.jpeg)

![](_page_37_Picture_0.jpeg)

**<u>Review</u>**